

Molecular Modeling and Simulation for Industrial Applications: Physico-Chemical Properties and Processes

Steady state molecular dynamics simulation of nucleation and droplet surface properties in a supersaturated vapor

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Classical nucleation theory

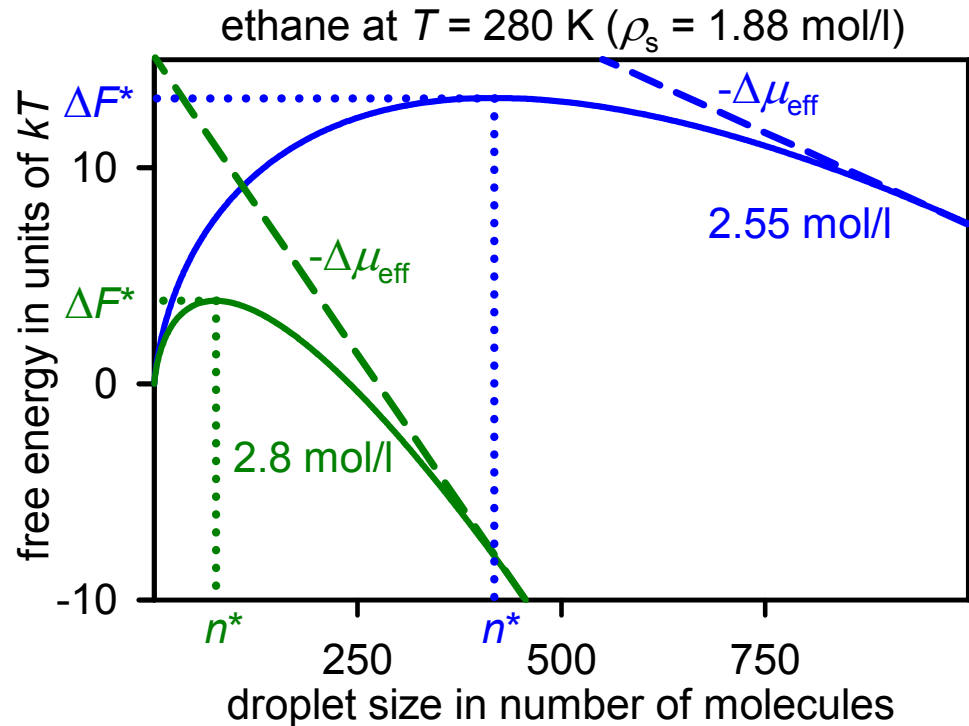
Free energy of formation

Positive surface contribution:

$$\left(\frac{\partial F_A}{\partial A_Y} \right)_T = \gamma (R_L^{-1}, T)$$

Negative bulk contribution:

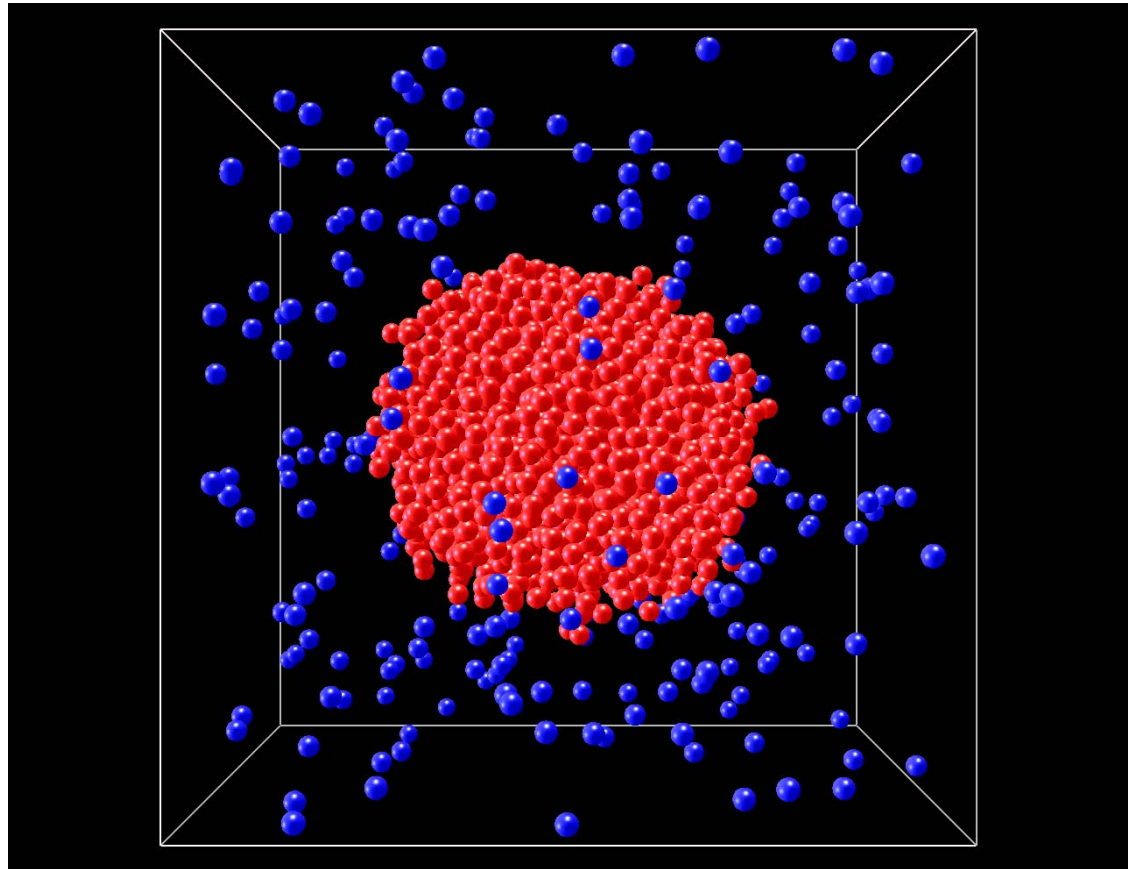
$$\left(\frac{\partial F_b}{\partial n} \right)_{N,V,T} = \mu^\ell - \mu + \frac{p - p^\ell}{\rho^\ell} = -\Delta\mu_{\text{eff}}$$



- I. The zero-curvature surface tension γ_0 is used instead of γ .
- II. The *pressure effect* is neglected, i.e. $\mu - \mu_s$ is used instead of $\Delta\mu_{\text{eff}}$.

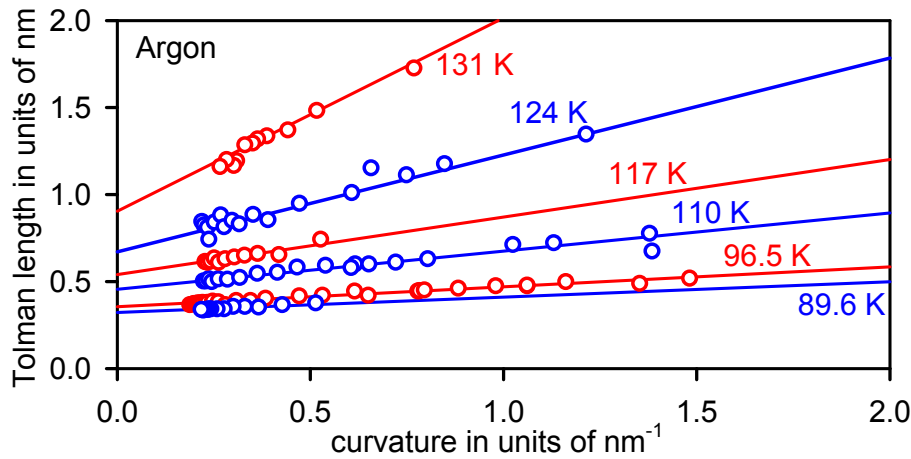
MD simulation of a single droplet

- Vapor and liquid are equilibrated separately
- A small ($n < 10\,000$) droplet is inserted into the vapor
- If the droplet cannot evaporate completely, an equilibrium is established within a few nanoseconds



truncated and shifted LJ potential ($r_c = 2.5 \sigma$)

Droplet surface tension



For small droplets, the Tolman length

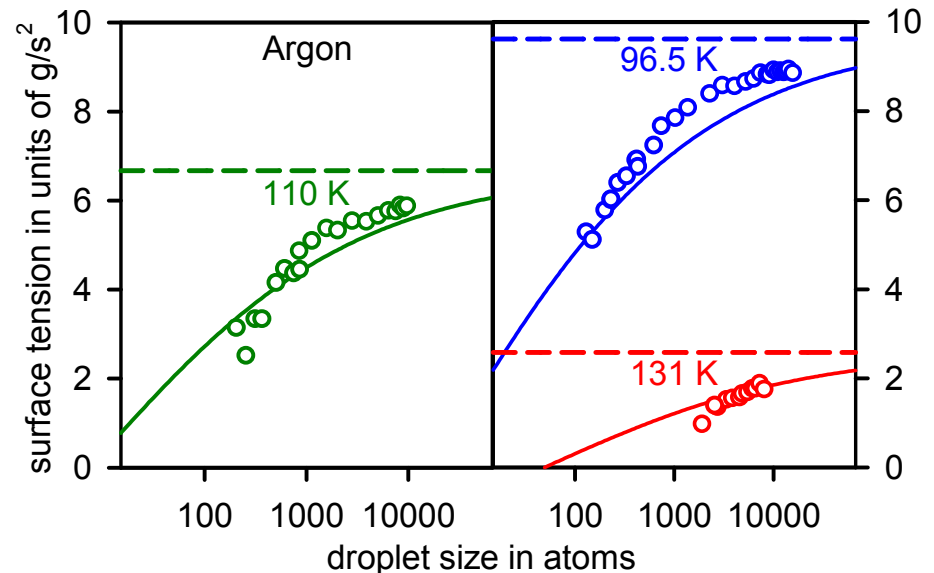
$$\delta = R_e - R_L$$

is significantly elevated.

Tolman equation:

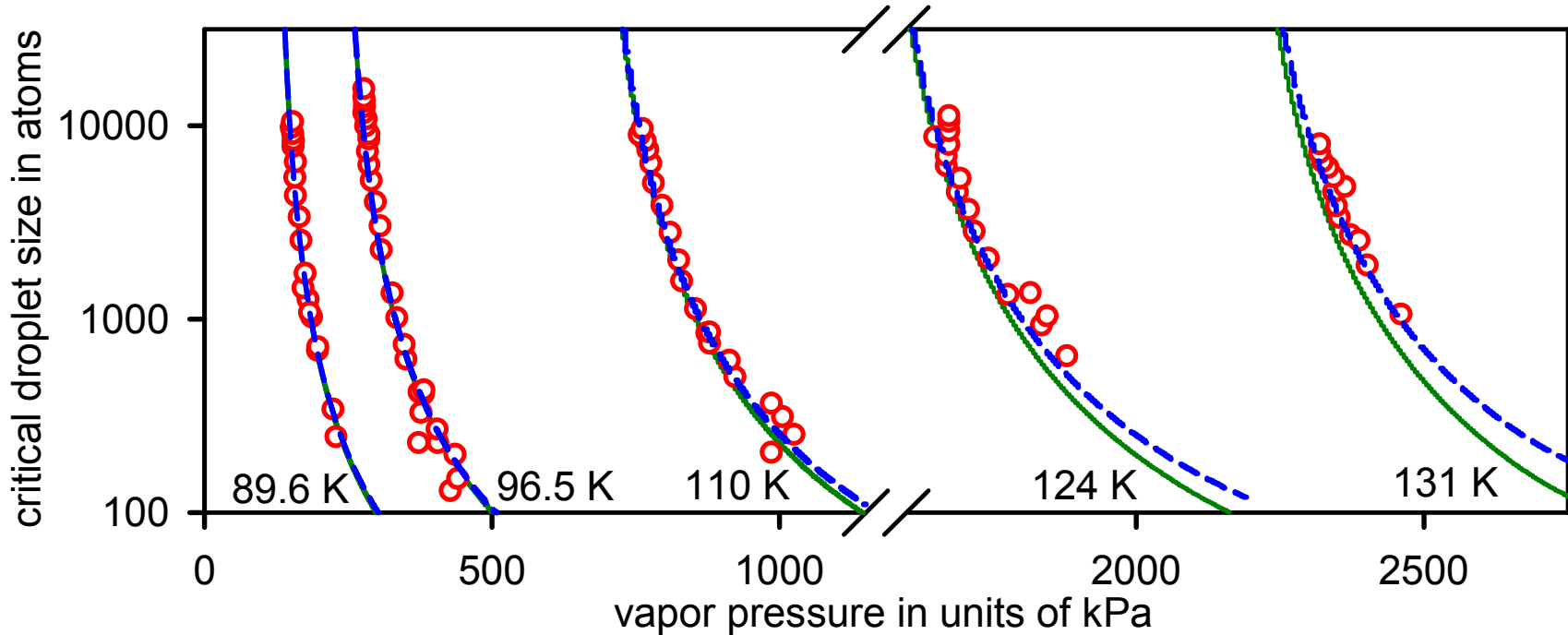
$$\frac{\gamma_0(T)}{\gamma} \approx 1 + 2\delta_0(T)R_L^{-1}$$

- MD simulation
- Tolman equation
- - - zero curvature



Single droplet in equilibrium

Argon (truncated-shifted LJ model)



———
 “standard”
 CNT

$$n^* = \left(\frac{2\gamma_0 a}{3(\mu - \mu_s)} \right)^3$$

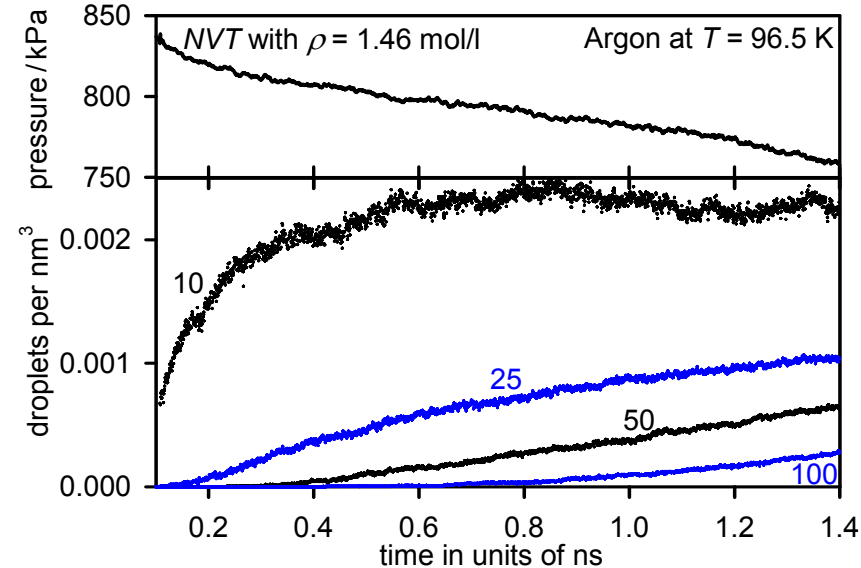
- - -
 CNT with the
 pressure effect

$$n^* = \left(\frac{2\gamma_0 a}{3\Delta\mu_{\text{eff}}} \right)^3$$

Direct MD simulation of nucleation

Yasuoka-Matsumoto method:

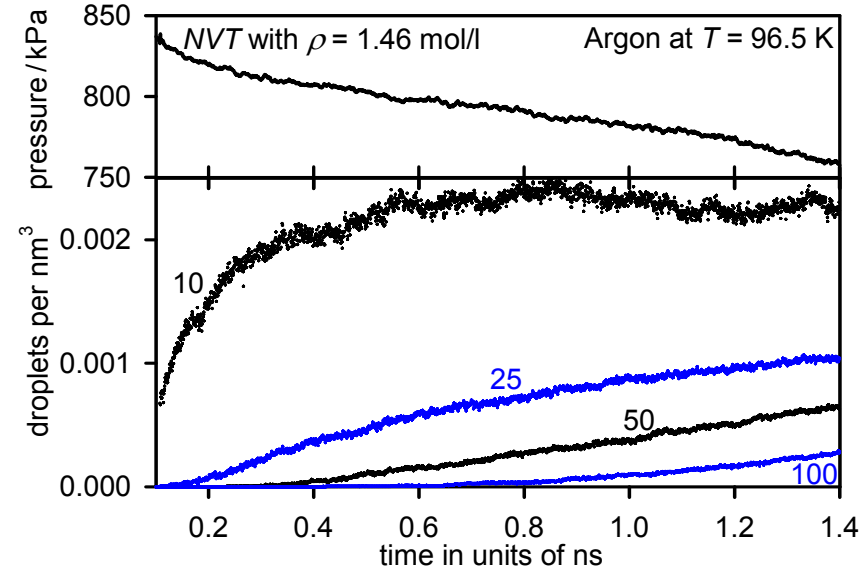
- Canonical MD simulation
- Limited time interval for nucleation
- **Conditions change over time**



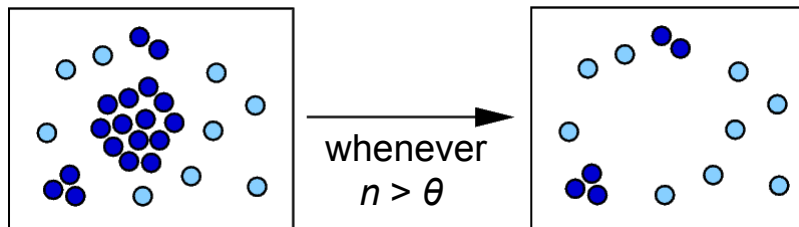
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GCMD, i.e. MD steps alternating with GCMC insertion/deletion steps

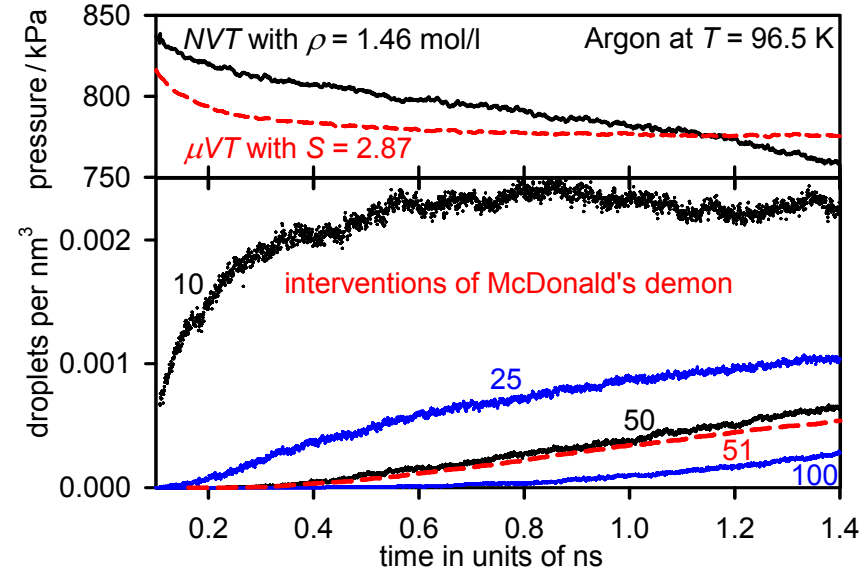


➔ Thermodynamic conditions of the supersaturated state are maintained

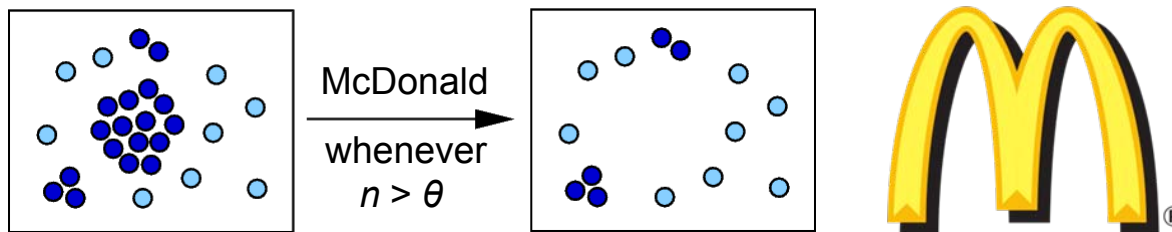
Direct MD simulation of nucleation

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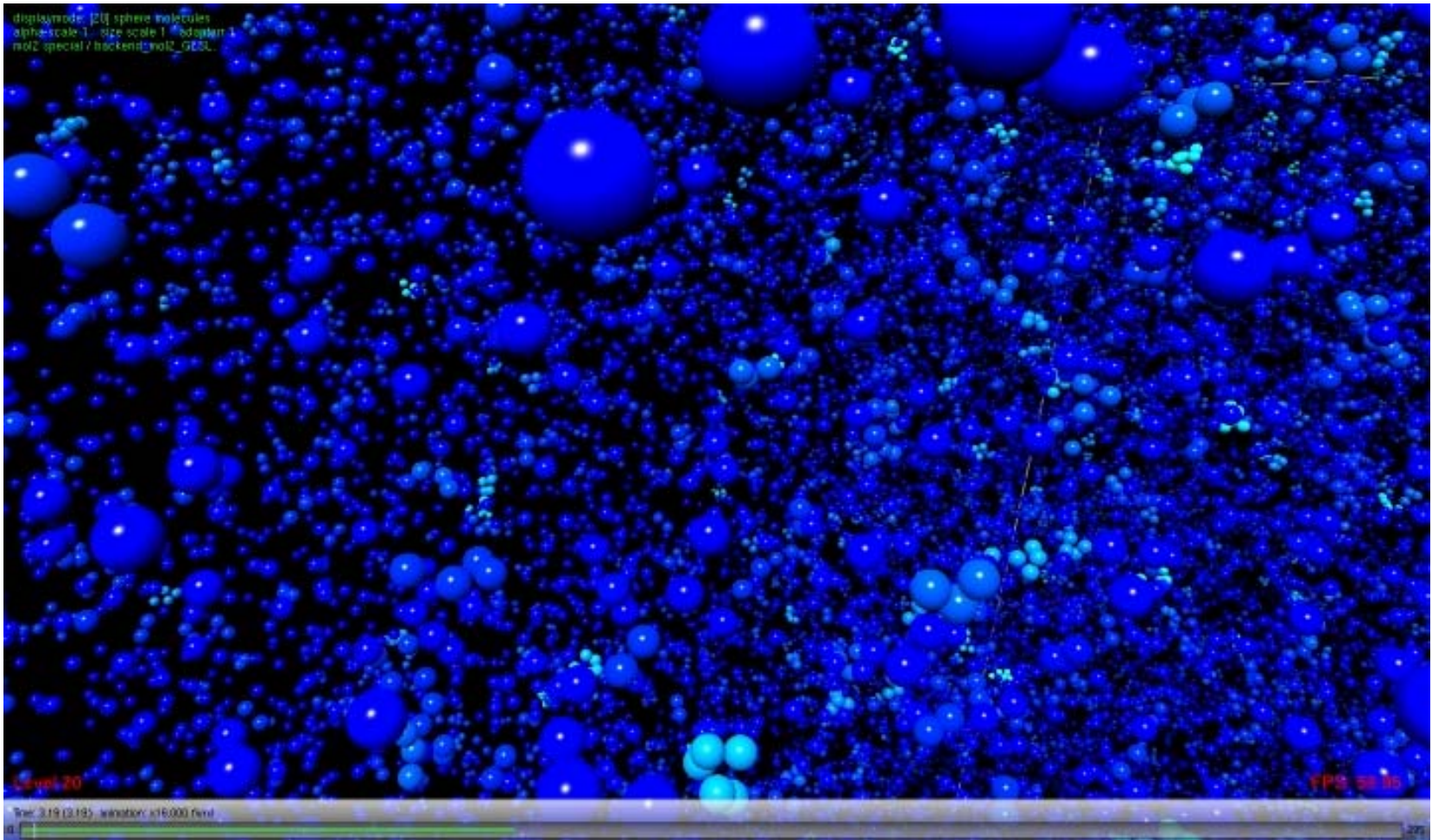


GCMD, i.e. MD steps alternating with GCMC insertion/deletion steps



➔ Thermodynamic conditions of the supersaturated state are maintained

Video: McDonald's demon



Intervention rate J_θ and nucleation rate J

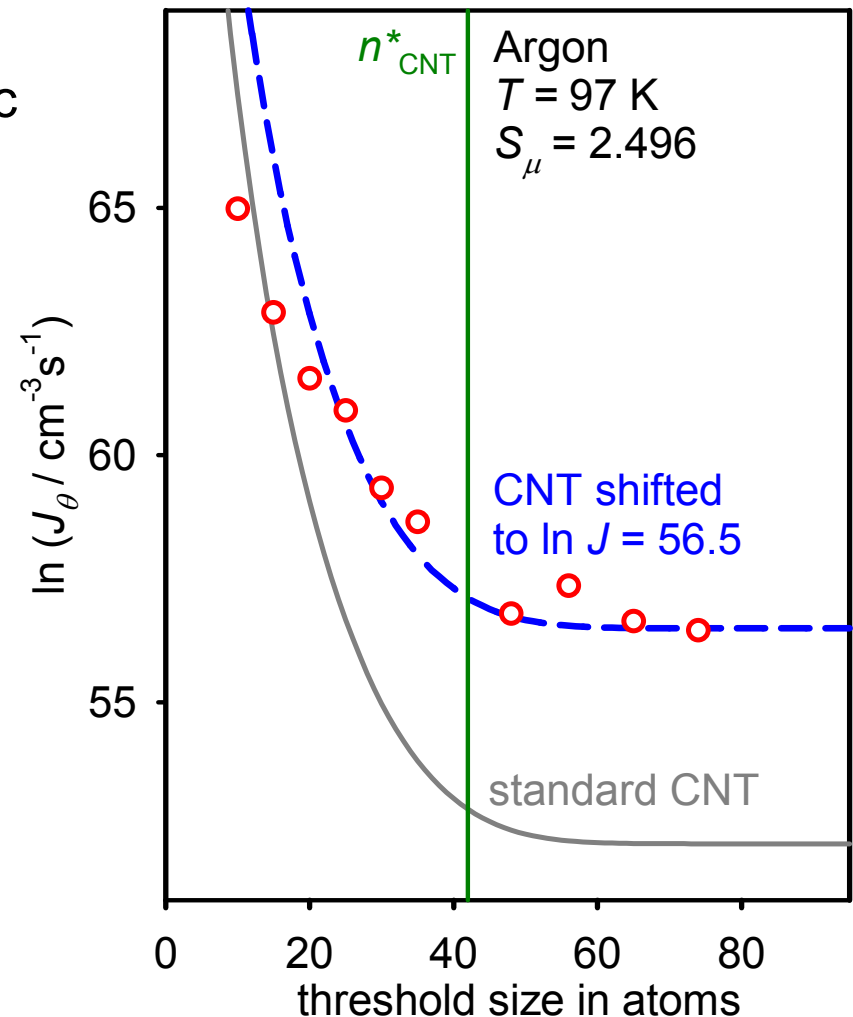
Not all of the removed droplets would eventually reach macroscopic size.

$$J = J_\theta q(\theta)$$

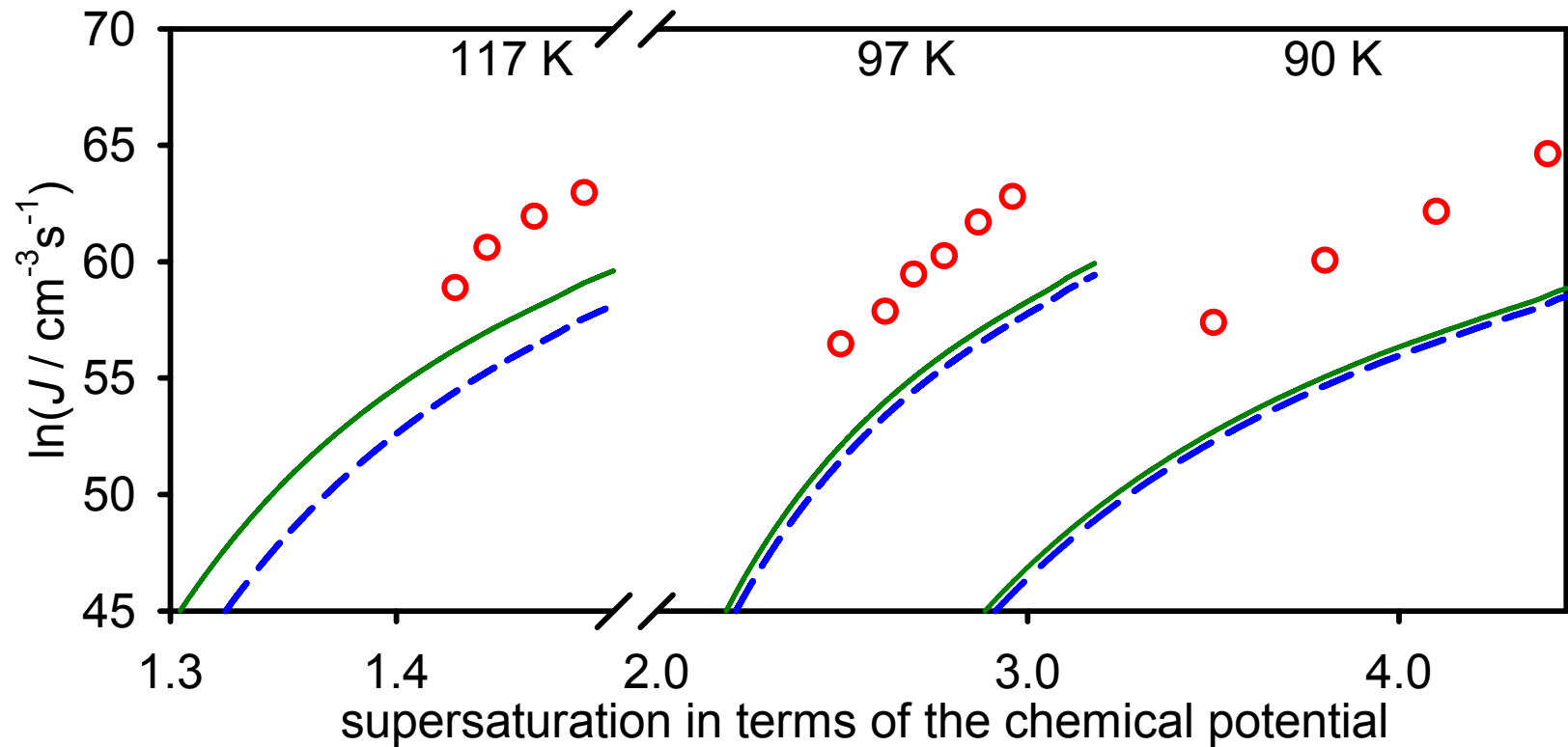
Probability for a droplet of growing from size θ to infinity:

$$q(\theta) = \frac{\int_1^\theta dn \exp(2F / kT)}{\int_1^\infty dn \exp(2F / kT)},$$

and in particular: $q(n^*) \approx 1/2$



GCMD simulation of nucleation: Results



- standard CNT
- - - CNT with the pressure effect
- GCMD with McDonald's demon

The thermodynamic surface of tension

The *surface tension* γ corresponds to a *surface of tension* A_γ with

$$\gamma = \left(\partial F_A / \partial A \right)_T.$$

Equilibrium condition for critical droplets yields $2 dV = R_L dA_\gamma$ and hence

$$dA_\gamma = \frac{2dn}{\rho R_L} \approx \frac{8\pi R_e^2}{R_e - \delta} dR_e.$$

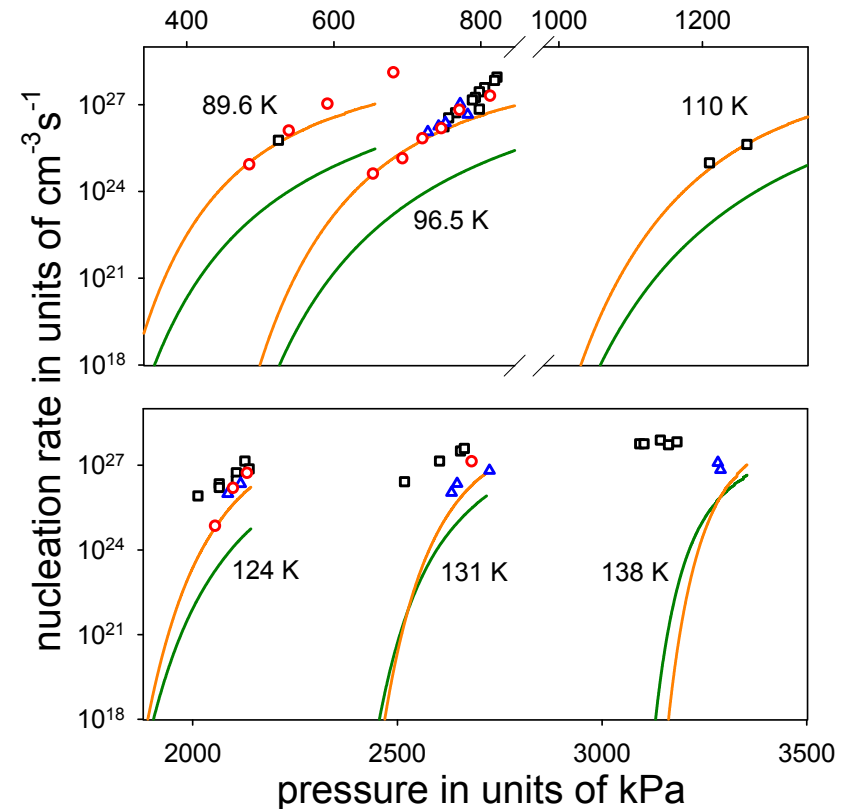
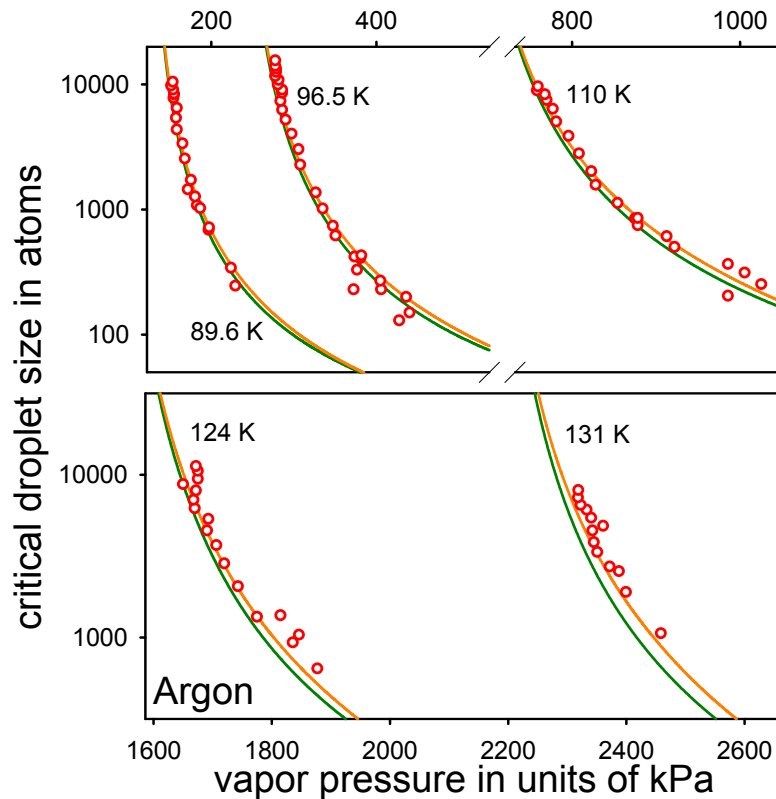
δ is positive \longrightarrow dA_γ is larger than according to capillarity approximation.

Postulated surface area deviates from the incompressible spherical case by

$$A - A_{\text{cap}} = \frac{0.85(1 - T/T_c)^{-1} - 1}{(n/75)^{1/3} + 1} A_{\text{cap}}.$$

Surface property corrected nucleation theory

Hypothesis: A larger surface area compensates the lower surface tension.



○ steady-state simulation

□ △ YM simulation

— SPC

— CNT

Conclusion

- MD simulation of **equilibria** allows sampling over an arbitrary time interval, eventually leading to the desired level of accuracy.
- **Single droplets** can be stable in the **canonical** ensemble.
- A **supersaturated vapor** near the spinodal line can be stabilized by grand canonical simulation with **McDonald's demon**.
- The **classical theory** leads to acceptable results for argon/LJ. However, it does not take into account curvature effects on the surface tension.
- Explanation: an **increased surface area** compensates the reduction of the surface tension due to curvature effects.